



JOINT RECORD OVERLAP

HOW PRIVATE RECORD MATCHING WORKS

THE SCENARIO

A retail chain (ShopMart) and a payment processor (PayFlow) want to know how many customers they share. ShopMart has a loyalty program with 50,000 members. PayFlow processes cards for 200,000 merchants. Neither will hand over their customer list to the other.

THE PROBLEM

Knowing the overlap size is valuable for both sides. ShopMart wants to understand what percentage of its loyalty members also use PayFlow cards (potential co-branded offer). PayFlow wants to know how many of its cardholders shop at ShopMart (targeted cashback campaign). But sharing raw customer lists is a privacy and compliance violation.

HOW IT WORKS

STEP 1: EACH SIDE ENCODES THEIR RECORDS

ShopMart takes its customer list (names, emails, or hashed IDs) and turns it into a binary vector. Think of it as a long row of zeros and ones, where a 1 means "we have this record" and a 0 means "we don't."

ShopMart: [0, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, ...]

PayFlow does the same with its cardholder list:

PayFlow: [0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, ...]

Both vectors use the same slot assignment, so a customer that appears at position 5 in ShopMart's vector also appears at position 5 in PayFlow's vector.

STEP 2: ENCRYPT AND UPLOAD

Each side encrypts their binary vector locally using the JuLenny toolkit. The raw lists never leave their premises. Only encrypted data is uploaded to the platform.

STEP 3: THE PLATFORM COMPUTES THE OVERLAP

JuLenny multiplies the two encrypted vectors element by element and sums the result. All math happens on encrypted data.

```
ShopMart:  [0, 1, 0, 0, 1, 1, 0, 1, 0, 0, 1, ...]
PayFlow:   [0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, ...]
Product:   [0, 0, 0, 0, 1, 1, 0, 0, 0, 0, 1, ...]

Sum = 3
```

STEP 4: DECRYPT THE RESULT

The result (3 in this example) is released after both parties approve. Both sides now know they share 3 customers.

TWO VARIANTS

Count variant: returns a single number (how many records overlap). Neither side learns WHICH specific records matched. Good for sizing the opportunity before committing to a deeper collaboration.

Itemized variant: returns the full result vector showing exactly which positions matched. The viewing party can look up which of their own records overlapped. Good for building a co-marketing list or a joint campaign.

WHAT NOBODY LEARNS

- ShopMart never sees PayFlow's full cardholder list
- PayFlow never sees ShopMart's full loyalty member list
- Records that did NOT match are completely hidden
- JuLenny never sees either list, even during processing

USE CASES BEYOND RETAIL

This function works for any "how many do we share?" question between two organizations:

- **Cybersecurity:** Two firms compare their threat indicator databases to find common IOCs (indicators of compromise) without exposing their full intelligence
- **Manufacturing:** Two companies compare parts catalogs to find overlapping SKUs for joint procurement
- **Genomics:** Two biobanks compare gene variant databases to find shared research subjects
- **Finance:** Two portfolio managers compare holdings to find co-invested assets
- **HR / Recruiting:** Two companies compare candidate pools to find shared applicants (with consent)



TECHNICAL DETAILS

- **Scheme:** BFV (exact integer arithmetic, no rounding)
- **Multiplicative depth:** 1
- **Max records:** 8,192 per ciphertext (larger datasets require chunking)
- **Result:** exact integer count (count variant) or exact binary vector (itemized variant)